

Single phase transformer



**ASSIGN
BUSTER**

Transformer BEE2123 ELECTRICAL MACHINES Mohd Rusllim Bin Mohamed

Ext: 2080 A1-E10-C09 edu. my © MRM 05 Learning

Outcomes ? At the end of the lecture, student should to: ? Understand the principle and the nature of static machines of transformer. Perform an analysis on transformers which their principles are basic to the understanding of electrical machines. ? © MRM 05 Introduction ? ? ? ? A transformer is a static machines. The word „ transformer? comes form the word „ transform?.

Transformer is not an energy conversion device, but is a device that changes AC electrical power at one voltage level into AC electrical power at another voltage level through the action of magnetic field, without a change in

frequency. It can be either to step-up or step down. Transmission System

TX1 TX1 Generation Station 33/13. 5kV 13. 5/6. 6kV Distributions TX1 TX1 ©

MRM 05 6. 6kV/415V Consumer Transformer Construction ? Two types of

iron-core construction: a) b) Core - type construction Shell - type

construction ? Core - type construction © MRM 05 Transformer

Construction ? Shell - type construction MRM 05 Ideal Transformer ? An ideal

transformer is a transformer which has no losses, i. e. it? s winding has no ohmic resistance, no magnetic leakage, and therefore no $I^2 R$ and core losses.

? However, it is impossible to realize such a transformer in practice. ? Yet, the approximate characteristic of ideal transformer will be used in

characterized the practical transformer. $N_1 : N_2$ $I_1 V_1$ E_1 E_2 $I_2 V_2$ V_1 -

Primary Voltage V_2 - Secondary Voltage E_1 - Primary induced Voltage E_2 -

secondary induced Voltage $N_1: N_2$ - Transformer ratio © MRM 05

Transformer Equation ? Faraday? s Law states that, ?

If the flux passes through a coil of wire, a voltage will be induced in the turns of wire. This voltage is directly proportional to the rate of change in the flux with respect of time. $V_{ind} = \text{Emf} = -N \frac{d\phi}{dt}$ Lenz's Law If we have N

turns of wire, $V_{ind} = \text{Emf} = -N \frac{d\phi}{dt}$ © MRM 05 Transformer

Equation For an ac sources, Let $V(t) = V_m \sin \omega t$ $i(t) = i_m \sin \omega t$ Since the flux is a sinusoidal function; $\phi(t) = \phi_m \sin \omega t$ Then: Therefore: $\frac{d\phi}{dt} = \omega \phi_m \cos \omega t$

$V_{ind} = \text{Emf} = -N \frac{d\phi}{dt} = -N \omega \phi_m \cos \omega t$ Thus: $V_{ind} = \text{Emf}_{ind}(\max) = N \omega \phi_m$

$2 \pi f N \phi_m$ © MRM 05 Emf ind (rms)

Transformer Equation For an ideal transformer $E_1 = 4.44 f N_1 \phi_m$

..... (i) In the equilibrium condition, both the input power will be equaled to the output power, and this condition is said to ideal condition of a transformer.

$E_2 = 4.44 f N_2 \phi_m$ Input power = output power $V_1 I_1 \cos \theta = V_2 I_2 \cos \theta$

$V_1 I_1 = V_2 I_2$ From the ideal transformer circuit, note that, $E_1 = V_1$

and $E_2 = V_2$ Hence, substitute in (i) © MRM 05 Transformer Equation

Therefore, $E_1 N_1 I_2 = E_2 N_2 I_1$ Where, „ a“ is the Voltage

Transformation Ratio; which will determine whether the transformer is going

to be step-up or step-down For $a > 1$ For $a < 1$ © MRM 05

Step-down Step-up Transformer Rating Transformer rating is normally

written in terms of Apparent Power. Apparent power is actually the product of its rated current and rated voltage. $V_A = V_1 I_1 = V_2 I_2$ Where, I_1 and I_2

= rated current on primary and secondary winding. V_1 and V_2 = rated

voltage on primary and secondary winding. Rated currents are actually the

full load currents in transformer © MRM 05 Example 1. 1. 5kVA single phase

transformer has rated voltage of 144/240 V. Finds its full load current.

Solution 1500 I1FL ? ? 10. 45 A 144 1500 I 2 FL ? ? 6A 240 © MRM 05

Example 2.

A single phase transformer has 400 primary and 1000 secondary turns. The net cross-sectional area of the core is 60m². If the primary winding is connected to a 50Hz supply at 520V, calculate: a) The induced voltage in the secondary winding b) The peak value of flux density in the core Solution N1= 400 V1= 520V A= 60m² N2= 1000 V2=? © MRM 05 Example 2 (Cont) a) Know that, $N_1 V_1 = N_2 V_2$ $400 \cdot 520 = 1000 V_2$ $V_2 = 1300V$ b) Emf, $E = 4.44 fN \Phi_m$ $\Phi_m = \frac{E}{4.44 fN}$ $\Phi_m = \frac{520}{4.44(50)(400)}$ $\Phi_m = 0.976 \times 10^{-5} \text{ Wb / m}^2 \text{ (T)}$ © MRM 05 Example 3.

A 25kVA transformer has 500 turns on the primary and 50 turns on the secondary winding. The primary is connected to 3000V, 50Hz supply. Find: Full load primary and secondary current b) The induced voltage in the secondary winding c) The maximum flux in the core Solution VA = 25kVA N1= 500 V1= 3000V N2= 50 V2=? a) © MRM 05 Example 3 (Cont) a) Know that, $V_A = V_1 I_1$ $25 \times 10^3 = 3000 I_1$ $I_1 = 8.33 \text{ A}$ $V_1 = 3000$ b) Induced voltage, $N_1 I_2 = N_2 I_1$ $500 I_2 = 50 \cdot 8.33$ $I_2 = 83.3 \text{ A}$ $V_2 = 3000 \cdot \frac{50}{500} = 300V$ $I_2 = 83.3$ c) Max flux $E = 4.44 fN \Phi_m$ $300 = 4.44(50)(50) \Phi_m$ $\Phi_m = 27 \text{ mWb}$ © MRM 05

Practical Transformer (Equivalent Circuit) I1 R1 X1 Ic V1 RC Io I1 ' Im Load Xm E1 E2 V2 N1: N2 I2 R2 X2 V1 = primary supply voltage V2 = 2nd terminal (load) voltage E1 = primary winding voltage E2 = 2nd winding voltage I1 = primary supply current I2 = 2nd winding current I1? = primary winding

current I_o = no load current I_c = core current I_m = magnetism current R_1 = primary winding resistance R_2 = 2nd winding resistance X_1 = primary winding leakage reactance X_2 = 2nd winding leakage reactance R_c © MRM 05 = core resistance X_m = magnetism reactance Single Phase Transformer (Referred to Primary) ? Actual Method

I_1 R_1 X_1 I_c I_o I_2 ' I_m Load R_c X_m E_1 E_2 V_2 R_2 ' X_2 ' N_1 : N_2 I_2 V_1 ? N_1 ? R_2
 ' ? ? ? N ? R_2 ? ? 2? ? N_1 ? X_2 ' ? ? ? N ? X_2 ? ? 2? 2 2 OR R_2 ' ? a R_2 2 ? N ? '
 E_1 ? V_2 ? ? 1 ? V_2 ? N ? ? 2? | I_2 ' ? 2 a © MRM 05 OR V_2 ' ? aV_2 OR X_2 ' ? a_2

X_2 Single Phase Transformer (Referred to Primary) ? Approximate Method I_1

R_1 X_1 R_2 ' X_2 ' I_c V_1 R_c I_o I_2 ' I_m Load X_m E_1 E_2 N_1 : N_2 I_2 V_2 ? N ? R_2 ' ? ?
 1 ? R_2 ? N ? ? 2? ? N ? X_2 ' ? ? 1 ? X_2 ? N ? ? 2? 2 2 OR R_2 ' ? a R_2 2 OR X_2 ' ?
 a_2 X_2 ? N ? ' E_1 ? V_2 ? ? 1 ? V_2 ? N ? ? 2? | I_2 ' ? 2 a © MRM 05 OR V_2 ' ? aV_2

Single Phase Transformer (Referred to Primary) ? Approximate Method I_1

R_01 X_01

V_1 aV_2 In some application, the excitation branch has a small current

compared to load current, thus it may be neglected without causing serious

error. ? N ? R_2 ' ? ? 1 ? R_2 ? N ? ? 2? ? N ? X_2 ' ? ? 1 ? X_2 ? N ? ? 2? 2 2 OR R_2 '

? a R_2 2 ? N ? ' V_2 ? ? 1 ? V_2 ? N ? ? 2? OR V_2 ' ? aV_2 OR X_2 ' ? a_2 X_2 R_01 ?

R_1 ? R_2 ' © MRM 05 X_01 ? X_1 ? X_2 ' Single Phase Transformer (Referred to

Secondary) ? Actual Method I_1 ' R_1 ' X_1 ' I_c I_o I_2 I_m X_m ' R_2 X_2 V_1 a R_c ' V_2 ? N

? R_1 R_1 ' ? ? 2 ? R_1 OR R_1 ' ? 2 ? N ? a ? 1? ? N ? X_1 ' ? ? 2 ? X_1 OR ? N ? ?

1? 2 2 ? N ? V V_1 ' ? ? 2 ? V_1 OR V_1 ' ? 1 ? N ? a ? 1? © MRM 05 X_1 ' ? X_1 a_2

Single Phase Transformer (Referred to Secondary) ? Approximate Method I_1 '

R_02 X_02 Neglect the excitation branch V_1 a V_2 R_02 ? R_1 ' ? R_2 X_02 ? X_1 ' ? X

R_1 OR R_1' ? X_1 OR X_1' ? N_1 ? a ? I_1 ? aI_1 © MRM 05
 X_1' ? X_1 a^2 Example 4. For the parameters obtained from the test of 20kVA
 2600/245 V single phase transformer, refer all the parameters to the high
 voltage side if all the parameters are obtained at lower voltage side side. R_c
 $= 3.3\Omega$, $X_m = j1.5\Omega$, $R_2 = 7.5\Omega$, $X_2 = j12.4\Omega$ Solution Given $R_c = 3.3\Omega$,
 $X_m = j1.5\Omega$, $R_2 = 7.5\Omega$, $X_2 = j12.4\Omega$ © MRM 05 Example 4 (Cont) i) Refer to
 H. V side (primary) E_1 V_1 2600 a ? ? ? 10.61 E_2 V_2 245 R_2' ? $a^2 R_2$ V_2
 $'$? aV_2 To refer parameters to primary, Use $R_2' = (10.61)^2 (7.5) = 844.$
 65Ω , $X_2' = j(10.61)^2 (12.4) = 1.396k\Omega$ R_c' and X_c' becoz parameters were
 read from secondary side $R_c' = (10.61)^2 (3.3) = 371.6\Omega$, $X_m' = j(10.61)^2$
 $(1.5) = j168.9\Omega$ © MRM 05 2nd I I2 ' ? 2 X2' ? a X2 a Example (What if..) 4.
 For the parameters obtained from the test of 20kVA 245/2600 V single phase
 transformer, refer all the parameters to the high voltage side if all the
 parameters are obtained at lower voltage side side.

$R_c = 3.3\Omega$, $X_m = j1.5\Omega$, $R_2 = 7.5\Omega$, $X_2 = j12.4\Omega$ Solution Given $R_c = 3.$
 3Ω , $X_m = j1.5\Omega$, $R_2 = 7.5\Omega$, $X_2 = j12.4\Omega$ © MRM 05 Power Factor ? Power
 factor = angle between Current and Voltage, $\cos \phi = V I / P = -ve$ Lagging ? V
 $I V ? = +ve$ Leading ? = 1 unity © MRM 05 Example 5. A 10 kVA single phase
 transformer 2000/440V has primary resistance and reactance of 5.5 Ω and
 12 Ω respectively, while the resistance and reactance of secondary winding is
 0.2 Ω and 0.45 Ω respectively. Calculate: i. ii. The parameter referred to high
 voltage side and draw the equivalent circuit The approximate value of
 secondary voltage at full load of 0.8 lagging power factor, when primary
 supply is 2000V. © MRM 05 Example 5 (Cont) Solution $R_1 = 5.5\Omega$, $X_1 = j12\Omega$?

$R_2 = 0.2 \Omega$, $X_2 = j0.45 \Omega$ i) Refer to H. V side (primary) $E = 2000 \text{ V}$
 $4.55 \text{ E}^2 V^2 440 I_1 R_01 9.64 V_1 X_01 21.32 \text{ a} V_2 R_2 = (4.55)^2 (0.2) = 4.14 \Omega$
 $X_2 = j(4.55)0.45 = j9.32 \Omega$ Therefore, $R_{01} = R_1 + R_2 = 5.5 + 4.13 = 9.64 \Omega$
 $X_{01} = X_1 + X_2 = j12 + j9.32 = j21.32 \Omega$ Example 5 (Cont)

Solution ii) Secondary voltage p. f = 0.8 $\cos \phi = 0.8 = 36.87^\circ$ 103VA

Full load, $I_{FL} = 5 \text{ A}$ 2000V From eqn. cct, $V_1 = I_1 (R_{01} + jX_{01}) + V_2$
 $2000 = (5)(9.64 + j21.32) + V_2$ $V_2 = 2000 - (4.5) V_2 = 422.6 \text{ V}$

0.80 © MRM 05 Transformer Losses i. ii. Generally, there are two types of

losses; Iron losses :- occur in core parameters Copper losses :- occur in

winding resistance i. Iron Losses $P_{iron} = P_c = (I_c)^2 R_c$ Popen circuit ii.

Copper Losses $P_{copper} = P_{cu} = (I_1)^2 R_1 + (I_2)^2 R_2$ Pshort circuit or if

referred, $P_{cu} = (I_1)^2 R_{01} + (I_2)^2 R_{02}$ © MRM 05 P_{oc} and P_{sc} will be

discusses later in transformer test Transformer Efficiency To check the

performance of the device, by comparing the output with respect to the

input. The higher the efficiency, the better the system. Efficiency, $\eta = \frac{\text{Output Power}}{\text{Input Power}}$

$\eta = 100\% \frac{P_{out}}{P_{in}} = 100\% \frac{P_{out}}{P_{out} + P_{losses}} = \frac{V_2 I_2 \cos \phi}{100\% V_2 I_2 \cos \phi + P_c + P_{cu}}$

$100\% \frac{V_2 I_2 \cos \phi}{V_2 I_2 \cos \phi + P_c + P_{cu}}$ (fullload) $\eta = \frac{(load \text{ n})}{VA \cos \phi} \times 100\%$

$\frac{VA \cos \phi}{VA \cos \phi + P_c + P_{cu}}$ $\eta = \frac{100\% \times nVA \cos \phi}{100\% \times nVA \cos \phi + P_c + P_{cu}}$ Where, if η load,

hence $n = \eta$, η load, $n = \eta$, 90% of full load, $n = 0.9$ Where $P_{cu} = P_{sc}$ $P_c = P_{oc}$

© MRM 05 $n_{max} = \frac{P_{oc}}{2 \sqrt{P_{sc} P_{oc}}}$ $V_{Arated} = \frac{P_{sc}}{I_{sc}}$

$V_{Arated} = \frac{P_{oc}}{I_{sc}}$ $V_{Arated} = \frac{P_{sc}}{I_{sc}}$ $V_{Arated} = \frac{P_{oc}}{I_{sc}}$

$V_{Arated} = \frac{P_{oc}}{I_{sc}}$ Voltage Regulation The measure of how well a power

transformer maintains constant secondary voltage over a range of load

currents is called the transformer's voltage regulation $\eta = \frac{P_{out}}{P_{in}}$

The purpose of voltage regulation is basically to determine the percentage of voltage drop between no load and full load. © MRM 05 Voltage Regulation ?

For calculation of Voltage Regulation, terminologies may be quite confusing, hence you need always think in current, I (A) point of view “ Full-load” means the point at which the transformer ? is operating at maximum permissible

secondary current ? When connected to load, current being drawn, hence

Voltage drop) ? ? No Load means at Rated At no load, current almost zero, so

takes Voltage at rated © MRM 05 value – think like an open circuit) Voltage

Regulation Voltage Regulation can be determine based on 3 methods: a) b)

c) Basic Definition Short – circuit Test Equivalent Circuit © MRM 05 Voltage

Regulation (Basic Defination) ? In this method, all parameter are being

referred to primary or secondary side. ? Can be represented in either ? Down

– voltage Regulation Note that: $V_{NL} ? V_{FL} V . R ? ? 100\% V_{NL}$ (at Rated

Value) $V_{NL} ? V_{FL} V . R ? ? 100\% V_{FL}$ © MRM

05 Voltage Regulation (Short – circuit Test) ? In this method, direct formula

can be used. $V . R ? V . R ? V_{sc} \cos ?? sc ? ? p . f ? V_1 ? 100\%$ If s/c test on

primary side $V_{sc} \cos ?? c ? ? p . f ? V_2 ? 100\%$ If s/c test on primary side Note

that: „-“ is for Lagging power factor „+“ is for Leading power factor Must

check that I_{sc} must equal to I_{FL} (I at Rated), otherwise © MRM 05 can? t use

this formula Voltage Regulation (Equivalent Circuit) ? In this method, the

parameters must be referred to primary or secondary $V . R ? I_1 R_{01} \cos ? p . f$

$? X_{01} \sin ? p . f V_1 I_2 R_{02} \cos ? p . f ? X_{02} \sin ? p . f V_2 ? ?? 100\% ?? 100\%$ If

referred to primary side $V . R ? ?$ If referred to secondary side Note that: „+“

is for Lagging power factor „-“ is for Leading power factor © MRM 05 assume

j terms ~ 0

Comment on VR ? Purely Resistive Load ? > 3 % is considered poor VR

Normally poor than Resistive Load ? Inductive Load ? ? Example of

application Desired Poor VR ? ? Discharge lighting AC arc welders © MRM 05

Example 6. In example 5, determine the Voltage regulation by using down –

voltage regulation and equivalent circuit. Question 5 A 10 kVA single phase

transformer 2000/440V and $V_1 = 0$ ($R_{01} = jX_{01}$) ($I_1 = ? ? o$) ? a $V_2 = 2000$

0 ? ($9.64 + j 21.32$) ($5 + j 36.87 o$) ? (4.55) $V_2 = 422.6 + 0.8o$ © MRM

05 Example Solution Down – voltage Regulation Know that, $V_{2FL} = 422.6V$

$V_{2NL} = 440V$ Therefore, V .

$R = V_{NL} - V_{FL} = 100\% V_{NL} - 440 - 422.6 = 17.4 = 3.95\%$ © MRM 05

Example 6 (Cont) Equivalent Circuit $I_1 = 5A$ $R_{01} = 9.64$ $X_{01} = 21.32$ $V_1 =$

2000V, 0.8 lagging p. f V . $R = I_1 R_{01} \cos \phi = 5 \times 9.64 \times 0.8 = 38.56$ $X = I_1 X_{01} \sin \phi = 5 \times 21.32 \times 0.6 = 63.96$

$V_1 = 2000 - 38.56 - j 63.96 = 1961.44 - j 63.96$ $V_2 = 1961.44 - j 63.96$ $V_2 = 1961.44 - j 63.96$ © MRM 05 Example A

short circuit test was performed at the secondary side of 10kVA, 240/100V

transformer. Determine the voltage regulation at 0.8 lagging power factor if

$V_{sc} = 18V$ $I_{sc} = 100$ $P_{sc} = 240W$ Solution Check: $I_{FL2} = I_{FL2} VA 10000 = 100$

$100 A$ $V = 100$? I_{sc} , Hence, we can use short-circuit method V . $R = V_{sc} \cos \phi_{sc}$

$sc = 18 \cos \phi_{sc}$ © MRM 05 ? 100% Example 7 (Cont) V . $R = V_{sc} \cos \phi_{sc}$? ? p.

$f = V_2 = 100\%$ Given p. f = 0.8 Hence, $\phi = \cos^{-1} 0.8 = 36.87 o$ Know

that , $P_{sc} = V_{sc} I_{sc} \cos \phi_{sc} = 18 \times 100 \times \cos \phi_{sc} = 240$ $\cos \phi_{sc} = 240 / (18 \times 100) = 0.8234$

$82.34 o$? $36.87 o$ V . $R = 18 \cos 82.34 o = 3.12$ © MRM 05 ? 12.62% ? ? 240 ? ? ? 82.

$34 o$? $\cos \phi = 1$? ? (18)(100) ? ? ? ? Example 8. The following data were

obtained in test on 20kVA 2400/240V, 60Hz transformer. $V_{sc} = 72V$ $I_{sc} = 8.$

$33A$ $P_{sc} = 268W$ $P_{oc} = 170W$ The measuring instrument are connected in the

primary side for short circuit test. Determine the voltage regulation for 0.8

lagging p. f. use all 3 methods), full load efficiency and half load efficiency. © MRM 05 Example 8 (Cont) $V \cdot R = V_{sc} \cos \phi_{sc}$ p. f = 0.8 Hence, $\cos \phi = 1 - 0.8 = 36.87\%$ o Know that, $P_{sc} = V_{sc} I_{sc} \cos \phi_{sc}$ $P_{sc} = I_{sc}^2 Z_{sc} \cos \phi_{sc}$ $V I_{sc} \cos \phi_{sc} = I_{sc}^2 Z_{sc} \cos \phi_{sc}$ $268 = I_{sc}^2 \cdot 63.4 \cdot 0.8$ $I_{sc} = 8.33$ $Z_{sc} = 8.64$ $63.4 = 3.86 + j 7.72$ $R_{01} = jX_{01}$ because connected to primary side. © MRM 05 Example 8 (Cont) 1. Short Circuit method, $V \cdot R = V_{sc} \cos \phi_{sc}$ p. f = 0.8 $V_1 = 100\%$ $72 \cos 63.4 = 36.87$ o $V \cdot R = 100\%$ 2.68% 2400 2. Equivalent circuit, V .

$R = I_1 R_{01} \cos \phi$ p. f = $X_{01} \sin \phi$ $V_1 = 100\%$ $20000 = 3.86(0.8) + 7.72(0.6) = 2400$ 100% 2.68% 2400 © MRM 05 Example 8 (Cont) 3. Basic Definition, $V_1 = I_1 Z_{01} = a V_2 = 20000 = 2400$ o $2400 = 0.79$ o $V_o = V_{NL} = V_{FL}$ $V \cdot R = 100\%$ $V_{NL} = 240 = 233.58$ 100% $240 = 2.68\%$ © MRM 05 Example 8 (Cont) (full load) $(1)(20000)(0.8) = 100\%$ 97.34% $2(1)(20000)(0.8) = 170$ $(1)(268)(0.5)(20000)(0.8) = 100\%$ 97.12% $2(0.5)(20000)(0.8) = 170$ $(0.5)(268)$ (half load) © MRM 05 Measurement on Transformer ? i. ii.

There are two test conducted on transformer. Open Circuit Test Short Circuit test ? ? ? The test is conducted to determine the parameter of the transformer. Open circuit test is conducted to determine magnetism parameter, R_c and X_m . Short circuit test is conducted to determine the copper parameter depending where the test is performed. If performed at primary, hence the parameters are R_{01} and X_{01} and vice-versa. MRM Open-Circuit Test ? ? V_{oc} I_c Measurement are at low voltage side $P_{oc} = V_{oc} I_c$

From a given test parameters, P_{oc} , V_{oc} , I_{oc} , $\cos \phi_{oc}$, $\sin \phi_{oc}$, I_c , I_m , R_c , X_m

Hence, $I_c = I_{oc} \cos \phi_{oc}$, $I_m = I_{oc} \sin \phi_{oc}$. Then, R_c and X_m , $V_{oc} = I_c R_c + I_m X_m$. Note: If the question asked parameters referred to high voltage side, the parameters (R_c and X_m) obtained need to be referred to high voltage side. © MRM 05 Short-Circuit Test

Measurement are at high voltage side. If the given test parameters are taken on primary side, R_{01} and X_{01} will be obtained. Or else, viceversa. $R_{01} = \frac{P_{sc}}{I_{sc}^2}$, $X_{01} = \frac{V_{sc}}{I_{sc}} - R_{01}$. Hence, $Z_{01} = \frac{V_{sc}}{I_{sc}}$. © MRM 05 For a case referred to Primary side $Z_{01} = R_{01} + jX_{01}$. Example 9.

Given the test on 500kVA 2300/208V are as follows: $P_{oc} = 3800W$, $P_{sc} = 6200W$, $V_{oc} = 208V$, $V_{sc} = 95V$, $I_{oc} = 52.5A$, $I_{sc} = 217.4A$. Determine the transformer parameters and draw equivalent circuit referred to high voltage side. Also calculate appropriate value of V_2 at full load, the full load efficiency, half load efficiency and voltage regulation, when power factor is 0.866 lagging. © MRM 05 [1392, 517.2, 0.13, 0.44, 202V, 97.74%, 97.59%, 3.04%] Example 9 (Cont) From Open Circuit Test, $P_{oc} = V_{oc} I_{oc} \cos \phi_{oc}$, $\cos \phi_{oc} = \frac{3800}{208 \times 52.5} = 0.696$, $\sin \phi_{oc} = \sqrt{1 - 0.696^2} = 0.717$. $I_c = I_{oc} \cos \phi_{oc} = 36.1A$, $I_m = I_{oc} \sin \phi_{oc} = 37.4A$. © MRM 05 Example 9 (Cont) Since $V_{oc} = 208V$ i.e. low voltage side, all readings are taken on the secondary side (low voltage side). $V_{oc} = 208V$, $R_c = \frac{P_{oc}}{I_c^2} = 11.39\Omega$, $I_c = 18.26A$, $V_{oc} = 208V$, $X_m = \frac{V_{oc}}{I_m} - R_c = 4.23\Omega$, $I_m = 49.21A$.

Parameters referred to high voltage side, $E_1 = 2300$ V, $R_c = 11$ Ω.

$X_m = 517$ Ω, $R_1 = 0.13$ Ω, $X_1 = 0.42$ Ω, $V_1 = 2300$ V, $I_{sc} = 217.4$ A, $P_{sc} = 6200$ W, $\cos \phi_{sc} = 0.866$.

Example 9 (Cont) From Short Circuit Test, First, check the I_{sc} and P_{sc} readings are actually taken on the primary side.

Since $I_{sc} = I_{FL}$, the readings are actually taken on the primary side.

$P_{sc} = I_{sc}^2 R_{01}$, $V_{sc} = I_{sc} Z_{01}$, $\cos \phi_{sc} = \frac{P_{sc}}{V_{sc} I_{sc}}$

$R_{01} = \frac{P_{sc}}{I_{sc}^2} = \frac{6200}{(217.4)^2} = 0.13$ Ω, $Z_{01} = \frac{V_{sc}}{I_{sc}} = \frac{2300}{217.4} = 10.58$ Ω

$X_{01} = \sqrt{Z_{01}^2 - R_{01}^2} = 10.42$ Ω, $\cos \phi_{sc} = 0.866$

Example 9 (Cont) Equivalent circuit referred to high voltage side,

$R_{01} = 0.13$ Ω, $X_{01} = 10.42$ Ω, $V_1 = 2300$ V, $I_1 = 217.4$ A, $P_{sc} = 6200$ W

Example 9 (Cont) For V_2 at full load, neglect the magnetism parameters,

$R_{01} = 0.13$ Ω, $X_{01} = 10.42$ Ω, $v_1 = 2300$ V, $v_2 = 240$ V, $\cos \phi = 0.866$

Example 9 (Cont) Efficiency, $\eta = \frac{P_{out}}{P_{in}} = \frac{P_{oc}}{P_{sc} + P_{oc}}$

$\eta = \frac{500 \times 103}{6200 + 500 \times 103} = 0.866$

$\eta = \frac{P_{oc}}{P_{sc} + P_{oc}} = \frac{3800}{6200 + 3800} = 0.9774$

$\eta = \frac{P_{oc}}{P_{sc} + P_{oc}} = \frac{3800}{6200 + 3800} = 0.9774$

Example 9 (Cont) Voltage Regulation, $V_{sc} \cos \phi_{sc} = V_1 - I_1 R_{01}$

$V_{sc} \cos \phi_{sc} = 2300 - 217.4 \times 0.13 = 2271.6$ V

$V_2 = \frac{V_{sc} \cos \phi_{sc}}{V_1} \times V_1 = \frac{2271.6}{2300} \times 240 = 235.4$ V

Example 9 (Cont) Test Yourself on Final Exam Q. Following are the test result of a 12

kV A, 415 V / 240 V, 50 Hz, two winding single phase transformer: Open

circuit test (reading taken on low voltage side) 240 V, 4.2 A, 80 W

Short circuit test (reading taken on high voltage side) 9.8 V, 28.9 A, 185 W

The values of R_p , R_s , X_p , X_s , X_m and R_c , assuming an approximate equivalent circuit.

ii. The efficiency of the transformer at full load and 0.8 lagging power factor.

iii. The voltage regulation at full load and 0.8 lagging power factor.

0.8 lagging power factor. © MRM 05 Solution i. Solution ? ? ? ? Eff = 97.3
% ? V. R = 2.31 % Z = 57.14 ? Rc = 714.3 ? Xm = 57.31 a = 1.73 R1 = 0.
11 ? R2 = 0.037 ? X1 = 0.13 ? X2 = 0.043 ? ? Refer to Primary, ? ? ? ? ? ©
MRM 05 Any Questions ??? Test 1 - coming soon Make sure you prepared for
that... © MRM 05